## SLIP-INDUCED DIRECTIONAL ORDER THEORY FOR B2-type superlattices



Fig. 6. Same as Fig. 5, except that emphasis is on *next-nearest-neighbor* pairs. (a) Undeformed state; all three  $\langle 100 \rangle$  NNN directions contain AA and BB pairs only. (b) to (d) Alternative arrangements after ( $\overline{1}12$ ) [ $1\overline{1}1$ ] slip, showing AB pairs (double bars) induced in all three  $\langle 100 \rangle$  directions.

Since  $\Delta N_{BB}$  occurs in [111], [ $\overline{1}$ 11] and [11 $\overline{1}$ ], we have from eqn. (1)

$$\cos^2 \varphi = (\cos^2 \varphi_{[111]} + \cos^2 \varphi_{[\overline{1}11]} + \cos^2 \varphi_{[\overline{1}11]})$$
$$= -\frac{2}{3}(\alpha_1 \alpha_2 - \alpha_2 \alpha_3 + \alpha_3 \alpha_1), \qquad (15)$$

which means that the  $[1\overline{1}1]$  slip direction is the effective direction of unlike pairs, which is a hard direction of magnetization for FeCo. In the general case, where the slip direction of slip system *i* has the direction cosines  $d_{1i}$ ,  $d_{2i}$ ,  $d_{3i}$ ,

$$\cos^2 \varphi_i = -2(d_{1i}d_{2i}\alpha_1\alpha_2 + d_{2i}d_{3i}\alpha_2\alpha_3 + d_{3i}d_{1i}\alpha_3\alpha_1)$$
$$\equiv -2f_i(\alpha_1, \alpha_2, \alpha_3).$$
(16)

The insertion of eqns. (14) and (16) into eqn. (1) then leads to

$$E = -\frac{1}{2}Nlp_0 p's^2 \sum_i |S_i| f_i(\alpha_1, \alpha_2, \alpha_3).$$
(17)

## (b) Short-range order case

For the short-range order case, the two nearestneighbor bonds associated with each  $\langle 111 \rangle$  direction (in a unit cell) contain a total of  $(1-\sigma)/2$  BB pairs in the undeformed state (see Appendix). After slip,  $\sigma = 0$  for the  $3\langle 111 \rangle$  directions other than the slip direction. Hence the gain in BB pairs in each of these directions is  $\sigma/2$ , or  $\sigma/2a^2\sqrt{6}$  per

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No. of slip system	Slip plane	Slip direction	2e <sub>xx</sub>	$2\varepsilon_{yy}$	2ε <sub>zz</sub>	$4\epsilon_{yz}$	4e <sub>zx</sub>	4ε <sub>xy</sub>	3 <i>d</i> <sub>1</sub> <i>d</i> <sub>2</sub>	3d <sub>2</sub> d <sub>3</sub>	3 <i>d</i> <sub>3</sub> <i>d</i> <sub>1</sub>
1	(112)	111	S <sub>1</sub>	<i>S</i> <sub>1</sub>	$-2S_{1}$	$-S_1$	$-S_1$	2S <sub>1</sub>	1	1	1
2	$(1\overline{2}1)$	111	S2	$-2S_{2}$	S2	$-S_2$	$2S_2$	$-S_2$	1	1	1
3	(211)	111	$-2S_{3}$	S <sub>3</sub>	S3	$2S_3$	$-S_3$	$-S_3$	1	1	1
4	(112)	111	S4	S4	$-2S_{4}$	S <sub>4</sub>	S4	$2S_4$	1	-1	-1
5	(121)	111	$-S_{5}$	2S5	$-S_5$	$-S_{5}$	2S5	S <sub>5</sub>	1	-1	-1
6	(211)	111	2S6	$-S_{6}$	$-S_6$	$2S_6$	$-S_6$	S <sub>6</sub>	1	-1	-1
7	(112)	Ī11	$-S_7$	$-S_{7}$	$2S_7$	S <sub>7</sub>	$-S_7$	2S <sub>7</sub>	-1	1	-1
8	(211)	Ī11	$-2S_{8}$	S <sub>8</sub>	S <sub>8</sub>	$2S_8$	S <sub>8</sub>	S <sub>8</sub>	-1	1	-1
9	(121)	Ī11	$-S_9$	$2S_9$	$-S_9$	So	2S9	$-S_9$	-1	1	-1
10	(211)	111	$2S_{10}$	$-S_{10}$	$-S_{10}$	$2S_{10}$	S10	$-S_{10}$	-1	-1	1
11	(121)	111	S11	$-2S_{11}$	S <sub>11</sub>	S11	$2S_{11}$	S11	-1	-1	1
12	(112)	111	$-S_{12}$	$-S_{12}$	2S <sub>12</sub>	$-S_{12}$	S <sub>12</sub>	2S <sub>12</sub>	-1	-1	1

TABLE III: VALUES OF  $\varepsilon$  and d (referred to cubic axes) for the twelve {112} (111) slip systems

TABLE IV: SUMMARY OF RESULTS BASED ON  $\{112\}$   $\langle 111 \rangle$  slip

Rolling plane	Rolling direction	Active slip systems	<i>S</i> <sub><i>i</i></sub>	E <sub>NN</sub>	Easy* axis
(001)	[110]	7,12	r/2	$\left(\frac{E_1 r}{6}\right) \alpha_1 \alpha_2$	TD
(115)	[110]	4,7,8,11,12	$ S_4  = 2r/27$	$\left(\frac{E_1r}{162}\right)(31\alpha_1\alpha_2+2\alpha_2\alpha_3+2\alpha_3\alpha_1)$	TD
			$ S_8  =  S_{11}  = 6r/27$ $ S_7  =  S_{12}  = 21r/54$	(102)	
(112)	[110]	4,7,8,11,12	r/3	$\left(\frac{E_1r}{18}\right)(3\alpha_1\alpha_2+\alpha_2\alpha_3+\alpha_3\alpha_1)$	RPN
(111)	[110]	4,7,8,11,12	$ S_4  = 2r/3$	$\left(\frac{E_1r}{54}\right)(5\alpha_1\alpha_2+6\alpha_2\alpha_3+6\alpha_3\alpha_1)$	RPN
(110)	[110]	1,4,7,12	$\begin{aligned}  S_8  &=  S_{11}  = 2r/9\\  S_7  &=  S_{12}  = 7r/18\\ r/2 \end{aligned}$	0	-

\* Relative among the three symmetry directions of rolled strip. TD-transverse direction, RPN-rolling plane normal.

unit {112} area. To this quantity we multiply by a factor  $(p'|S|/d=p'|S|\sqrt{6/a})$  as before, leading to the expression

$$\Delta N_{\rm BB} = p'|S| \left(\frac{\sqrt{6}}{a}\right) \left(\frac{\sigma}{2a^2\sqrt{6}}\right) = \frac{1}{4}Np'\sigma|S|.$$
(18)

Insertion of eqns. (16) and (18) into eqn. (1) then leads to

$$E = -\frac{1}{2}Nlp'\sigma\sum_{i}|S_{i}|f_{i}(\alpha_{1},\alpha_{2},\alpha_{3})$$
(19)

for the SRO case.

Finally, by combining the LRO and SRO expressions of eqns. (17) and (19), we obtain

$$E = -\frac{1}{2}E_1 \sum |S_i| f_i(\alpha_1, \alpha_2, \alpha_3), \qquad (20)$$

where  $E_1 = Nlp'(p_0 s^2 + \sigma)$  as before. Equation (20) is the expression for the slip-induced anisotropy energy developed by  $\{112\}\langle 111\rangle$  slip and based on NN interactions.

## (c) Applications to rolling

As in the treatment of  $\{110\}\langle 111\rangle$  slip in Part 2 above, eqn. (20) has been applied to rolling of (001)[ $\overline{1}10$ ], (115)[ $\overline{1}10$ ], (112)[ $\overline{1}10$ ], (111)[ $\overline{1}10$ ] and (110)[ $\overline{1}10$ ] orientations. For the convenience of calculations, the appropriate parameters (similar to

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